Application of the Random Coupling Model to Electromagnetic Statistics in Complex Enclosures

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Abstract—The effectiveness of the random coupling model (RCM) in predicting electromagnetic wave coupling to targeted electronic components within a complex enclosure is examined. In the short-wavelength limit with respect to the characteristic length of the enclosure, electromagnetic wave propagation within a large enclosure is sensitive to small changes to the interior, or to the boundaries of the enclosure. Such changes can reduce or invalidate the applicability of deterministic predictions of the electromagnetic fields at radiofrequencies (RF) in large enclosures. Under such circumstances, a statistical approach is needed to provide a better understanding of RF coupling to components within large enclosures. In this paper, we experimentally demonstrate the applicability of a statistical technique, the RCM, to estimate the probabilistic magnitudes of RF fields on electrically large components (i.e., long cables, etc.) that are partially shielded within a complex, 3-D enclosure.

Index Terms—Electromagnetic compatibility (EMC), overdetermined enclosures, probability density function, random coupling model (RCM), statistical electromagnetism, wave scattering.

I. INTRODUCTION

There is practical interest in the statistics of electromagnetic radiation affecting sensitive electronics that are shielded within a large enclosure, both in areas of electromagnetic compatibility (EMC) [1]–[6], and in defense-related radiofrequency (RF) attack scenarios. The RF coupling to targeted electronics within a large enclosure can be studied by considering a wave scattering problem in the short-wavelength limit. While the applied wavelength is short with respect to the characteristic length of the wave enclosure, electromagnetic field distributions in electrically large enclosures can vary dramatically even with a small rearrangement of the internal objects, a small change in the enclosure boundaries, or a change in frequency of the excitation waveform. At a particular location, the field may have contributions from a superposition of hundreds of excited modes [4], and therefore, the locations of field maximums and minimums are also very sensitive to such small changes. Power coupling of electromagnetic fields to a component, such as a conductor or an electronic device, in one enclosure may be quite different in another nearly identical enclosure. Therefore, deterministic calculations are valid only for the particular situation modeled. Under such circumstances, analysis of the statistical properties of electromagnetic fields in these complex environments is necessary, and the statistical predictions can better represent the properties of complex enclosures.

The statistical treatment of electromagnetic fields in cavities (wave enclosures) is a well-researched area beginning with Holland and St. John [7]. Traditionally, statistical electromagnetic techniques involve determining the electric field intensity at a particular location in a cavity or determining the overall field distribution in order to evaluate shielding effectiveness or to determine the EMC of devices. The technique described in this study does not determine statistical field strengths, but rather takes an “impedance approach” to calculate induced voltages on ports in a complex enclosure. These ports can be a traditional antenna like a monopole, pins on an integrated circuit, or wires or bundles of wires running inside a below-deck ship compartment. The statistical coupling of RF energy to wires and wire bundles has been approached with other techniques. For example, Langley adapts a vibroacoustic method, which breaks the coupling problem into random and deterministic components that can be analyzed separately: the wire is taken to be the deterministic component and the surrounding dielectric cavity the random component [8]. In this paper, the statistical treatment is the random coupling model (RCM) that is based on wave chaos and has been successfully applied to describe the statistics of many wave scattering properties [9]–[11]. Wave chaos is a field that studies wave propagation in ray-chaotic enclosures in the short-wavelength limit [6], [12]. A ray-chaotic enclosure means the dynamics of the ray trajectories in the enclosure is chaotic, so initial deviations of trajectories grow, on average, exponentially in time [13]. In a wave chaotic system, the statistical features of wave scattering properties have a universal fluctuation part and a system-specific deterministic part. The universal fluctuation part is well-predicted by random matrix theory (RMT) [14], and the RCM combines the system-specific deterministic part with the universal fluctuation part in an impedance approach [15], [16]. It
is conjectured that this wave chaos model, the RCM, can be applied to complex wave enclosures that are complicated enough in the short-wavelength limit such that the universal fluctuation feature is valid.

Previously, the RCM has been applied to predict RF field coupling through antennas of subwavelength dimension, into a quasi-2-D, ray-chaotic microwave cavity, [9], [11], [17], and a 3-D computer box [9], [11]. This paper extends the work of Hem mad y et al. by examining the applicability of the RCM to a large, complex cavity, which has a short monopole antenna and a long antenna that is much larger than the wavelength. The short antenna represents a wave transmitting port. The long antenna is a 0.92-m long U-shaped conductor used as a receiving port and it represents a long piece of cable, or a bundle of wires, which could lead to a below-deck ship compartment that could be susceptible to picking up unwanted RF radiation. This could be useful for predicting damage due to an RF attack. The RCM has never been tested in the wave system with a multiple-wavelength-long port. Additionally, this study presents novel results, which show that the RCM predictions of induced voltages on a receiving port are independent of the transmitting port location.

This paper is organized as follows. In Section II, the theoretical approach of the RCM is briefly summarized. Section III details the experimental setup, and how the loss parameter (α) of the cavity is experimentally determined. The loss parameter determines the statistical distributions predicted by RMT and will be further introduced. Section IV presents experimental results that show that the RCM is applicable to a complex 3-D cavity, with an electrically large receiver port. The following four results are obtained: 1) the universal fluctuation part of the experimental data agrees with the prediction of RMT; 2) the system-specific feature can be described by the RCM; 3) the RCM prediction of the probability density function (PDF) of induced voltages on the long port matches the experimental data; and 4) the distribution of induced voltages on the electrically large port is independent of the transmitting port location. Finally, Section V summarizes the implications of these results.

II. THEORY

The RCM is a statistical model that combines universal statistical properties of a wave chaotic system with system-specific features of the system to predict statistical properties of electromagnetic fields in a complex enclosure. The RCM is derived in the impedance domain and can predict the statistics of the impedance matrix and the scattering matrix of the system. Most importantly for the applications of EMC, the RCM predicts the PDF of induced voltages on target objects (ports) inside a complex enclosure [9], [11].

We are interested in comparing these predicted induced voltage PDFs with experimentally determined PDFs. The experimental-induced voltage is calculated from elements of the impedance matrix, which describes the linear relationship between the voltages at the ports and the currents at the ports. The measurement of a multiport complex cavity is typically carried out by obtaining the scattering matrix, S, which may be transformed to an equivalent impedance matrix, Z, obtained through the standard bilinear relationship

\[ Z = Z_0^{1/2} (I + S)(I - S)^{-1}Z_0^{1/2} \]

where \( Z_0 \) is a diagonal matrix of the characteristic impedances of the waveguides connected to the ports of the cavity and \( I \) is the unit matrix. For a two-port system, all of these matrices are \( 2 \times 2 \) matrices. Hart et al. show that the statistics of the impedance matrix, \( Z_{cav} \), of a multiport complex cavity can be decomposed into parts that describe the universal (fluctuating) and system-specific (deterministic) properties of the cavity as [17], [18],

\[ Z_{cav} = j \text{Im}[(Z_{cav})] + \text{Re}[(Z_{cav})]^{1/2} z \text{Re}[(Z_{cav})]^{1/2}. \]

The matrix \( \langle Z_{cav} \rangle \) is called the ensemble-averaged cavity impedance matrix, which captures the system-specific features of the cavity [17]. \( \text{Re}[-] \) and \( \text{Im}[-] \) mean taking the real part and the imaginary part, respectively. The ensemble-averaged impedance matrix \( \langle Z_{cav} \rangle \) is calculated by taking the average of the impedance matrices \( Z_{cav} \) over a finite number of configurations of the cavity. In this paper, we measured 200 different \( 2 \times 2 \) impedance matrices [obtained from the cavity scattering matrices using (1)], and the technique for generating different configurations of the cavity is discussed in Section III-A.

According to the RCM and previous experimental verifications [17], [18], \( \langle Z_{cav} \rangle \) approximates the radiation impedance matrix, \( Z_{rad} \), plus the short-trajectory coupling between the ports. The matrix \( Z_{rad} \) represents the radiation and near-field characteristics of the ports, and can be measured by retaining the near-field properties of the port and establishing boundary conditions so that no waves ever return to the port (i.e., placing an absorber on the walls of a cavity); \( Z_{rad} \) can also be calculated. The short-trajectory coupling refers to either line-of-sight contributions between two ports or contributions made by ray trajectories that have made a few reflections inside the enclosure before coupling to the port [17], [18]. Both the radiation impedance matrix and the short-trajectory coupling are system-specific features, and are included in \( \langle Z_{cav} \rangle \).

On the other hand, the universal fluctuating part is called the normalized impedance matrix

\[ z = (\text{Re}[\langle Z_{cav} \rangle])^{-1/2} \left(\langle Z_{cav} \rangle - j \text{Im}[\langle Z_{cav} \rangle]\right) (\text{Re}[\langle Z_{cav} \rangle])^{-1/2} \]

whose statistical properties are predicted by the RMT. The normalized impedance matrix describes the universal fluctuation properties of the measured impedance \( Z_{cav} \) [15], [16]. The statistics of all of the elements of the matrix \( z \) only depend on the loss parameter, \( \alpha \), of the system [9], [11]. The definition of the loss parameter and how to determine \( \alpha \) by using experimental data will be further discussed in Section III-B. In a short summary, the RCM can model the statistics of \( Z_{cav} \) by using the measured system-specific feature \( \langle Z_{cav} \rangle \) and the statistical properties of \( z \), which is obtained by using the RMT and the single parameter, \( \alpha \). Consequently, the RCM can predict the statistics of the induced voltages on a target in a wave chaotic enclosure. The result is shown in Section III-C.
III. EXPERIMENTAL SETUP AND DATA ANALYSIS

A. Experimental Setup

We test the application of the RCM in modeling the wave coupling to targeted electronic components within a complex enclosure, which is shown in Fig. 1. The complex enclosure, called the GigaBox, is a reverberation chamber (rectangular aluminum box with dimensions of 1.22 m × 1.27 m × 0.65 m). There are mode stirrers (scatterers) made of aluminum inside the GigaBox, and the mode stirrers can be systematically rotated to 200 discrete orientations. It also has an irregular internal surface. The mode stirrers and the irregularities on the internal surface facilitate the creation of ray-chaotic trajectories inside the enclosure, and the elimination of degenerate modes.

The GigaBox has two ports. Port 1 is a monopole antenna with a physical length of 1.3 cm. The monopole antenna is internally mounted on a vertical wall of the GigaBox. Port 2 is a U-shaped conductor representing a long cable. The U-shaped conductor is a copper tube of 0.6-cm diameter. It is internally mounted on another wall of the GigaBox, which is orthogonal to the wall that carries the monopole antenna (port 1). The U-shaped conductor has a total length of 115.6 cm, and it has a 90.2-cm long portion that is parallel to the wall of the GigaBox at a distance of 12.7 cm from the wall. One end of the U-shaped conductor (port 2) is terminated with a 50-Ω load while the other end is connected to a network analyzer, and port 1 is also connected to the network analyzer as shown in the Fig. 1. The network analyzer measures the scattering matrix of the GigaBox as a 2 × 2 matrix, whose elements (denoted as $S_{11}$, $S_{12}$, $S_{21}$, and $S_{22}$) are complex functions of source frequency.

A large number of configurations of the cavity are required to achieve a randomized electromagnetic environment [19]. The mode stirrers inside the GigaBox are rotated to 200 different orientations to create 200 configurations of the GigaBox. These configurations of the GigaBox have the same volume and quality factor; however, their boundary conditions are different. Experiment has taught us that it is actually much fewer than 200 samples needed to provide a sufficient statistical ensemble, but we had the physical capability to have 200 realizations, so we used that amount. The scattering matrix is measured for each configuration over the frequency range 3–10 GHz, where the wavelength $\lambda$ is small compared to the enclosure size. (A rule of thumb is to use $\lambda \ll \sqrt{V}$, where $V$ is the volume of the enclosure.) In the short-wavelength limit, there is significant perturbation between each configuration, and an autocorrelation analysis showed that the 200 measured realizations are highly uncorrelated samples.

B. Determination of the Loss Parameter of the GigaBox

As described in Section II, determination of the loss parameter of the cavity is essential to apply the RCM. In the frequency spectra of the transmitted or reflected signals of a complex wave enclosure, one can see separately distributed resonances over the measured frequency window. The dimensionless loss parameter, $\alpha$, is defined as the ratio of the 3-dB (half-power) bandwidth of the closed-cavity mode resonance to the mean spacing between cavity modes (eigenmodes), $\alpha \equiv f/(2Q\Delta f)$. Here, $f$ is the frequency, $\Delta f$ is the mean spacing of adjacent eigenfrequencies, and $Q$ is the typical (unloaded) quality factor of the cavity, which may be measured in several ways, one of which is to use $Q = 2\pi f\tau$, where $1/\tau$ is the rate of voltage decay in the cavity. The mean spacing of the eigenmodes may also be measured directly from the $S_{21}$ (transmission) response of the cavity. Note that $\alpha$ is independent of the ports and is a property of the closed cavity which has eigenmodes and eigenfunctions dictated by the solutions of the wave equation. For an open system, such as the GigaBox, where waves access the enclosure from outside, we consider an equivalent closed system in which uniform absorption accounts for wave energy lost from the system, and we assume that we can define an equivalent loss parameter for the open system [9], [11]. The loss parameter, $\alpha$, is the only parameter needed to describe the statistics of the universal properties of a wave-chaotic system. Hemmady has discussed several different methods for determining $\alpha$ in Appendix B of his thesis [9]. For example,
\[ \alpha = \frac{k^3 V}{2\pi^2 Q} \]  

in a 3-D cavity, where \( k \) is the wave number, \( V \) is the cavity volume, and \( Q \) is average cavity quality factor. This method works well when one knows or can estimate \( Q \) and \( V \). Another method is to compare PDFs of the real and imaginary parts of the experimental normalized impedance matrix, \( Z \), with the predicted PDFs of the RMT by using \( \alpha \) as a fitting parameter [9], [14].

Instead of comparing the whole PDF, when the loss is high enough (\( \alpha > 1 \)), \( \alpha \) can be estimated by only using the variance of elements of the normalized impedance matrices, \( Z \), from different configurations of the cavity [9], [20]. For example, the relationship of the variance of the off-diagonal elements of \( Z \) and the loss parameter is

\[
\alpha = \frac{1}{2\pi \sigma_{\text{Re}[Z_{ij}]}^2} = \frac{1}{2\pi \sigma_{\text{Im}[Z_{ij}]}^2}.
\]

Here, \( \sigma^2 \) is the variance, \( \text{Re}[Z_{ij}] \) and \( \text{Im}[Z_{ij}] \) denote the real and imaginary parts of the off-diagonal components of the 2 \( \times \) 2 normalized impedance matrix, \( Z \). We refer to this method used to determine the loss parameter as “the variance method,” and it is the method used in this paper. Values of \( \alpha \) obtained by the variance method are presented in Table I.

The loss parameter, \( \alpha \), is a smoothly varying function of frequency and is not expected to vary widely over small bandwidths such as 100 MHz as chosen in Table I. For a 100-MHz window, the average number of resonances is from 800 (in 3.0–3.1 GHz) to 8800 (in 10.0–10.1 GHz), and the number of points is set as 16 001 for the network analyzer.

### IV. Experimental Results

#### A. Applicability of the RMT to Universal Fluctuations in the GigaBox

We first examine the statistics of the normalized impedance matrix \( Z \) in (3)) to see if they agree with the predictions of the RMT. In order to carry out the normalization, the matrix \( \langle Z_{\text{cav}} \rangle \) was computed by taking the average of the measured \( Z_{\text{cav}} \) matrices over the 200 configurations; these \( Z_{\text{cav}} \) matrices were obtained from scattering matrix measurements. Next, the normalized impedance, \( Z \), was determined for each of the 200 measured \( Z_{\text{cav}} \) matrices by solving (3).

Each of these \( Z \) matrices has complex diagonal elements. The PDFs of the real and imaginary parts of these diagonal elements are shown in Fig. 2. In Fig. 2, the PDFs, which were generated solely from the experimental data, are compared with PDFs, which were generated using the RMT.

The RMT offers a Monte Carlo method to generate random impedance matrices, \( Z_{\text{RMT}} \), whose statistics are the same as the statistics of the normalized impedance matrix, \( Z \). The random matrix can be generated as [9], [11]

\[
z_{\text{RMT}} = -\frac{j}{\pi} W (\Lambda - j \alpha I)^{-1} W^T \]

where \( \Lambda \) is the random matrix of resonances (eigenmodes of the closed system), \( I \) is the unit matrix with the same size as \( \Lambda \), and \( W \) is the random matrix of the port coupling. \( W^T \) is the transpose matrix of \( W \). To represent an overmoded wave system, such as the complex enclosure in the short-wavelength limit, one needs to generate \( \Lambda \) as a large \( M \times M \) matrix, where \( M \) is the number of eigenmodes and \( M > 1000 \). \( W \) is also a numerical generated random matrix with the size \( N \times M \), where \( N \) is the number of ports. The rules of generating the random matrices \( \Lambda \) and \( W \) are indicated by the RMT [9], [14], [16], and they are out of scope of this paper. Note that the loss parameter \( \alpha \) is the only parameter determining the statistics of the elements of \( \langle Z_{\text{RMT}} \rangle \).

Fig. 2 shows PDFs of the real and imaginary parts of \( z_{11} \) for both experimental and theoretical (RMT) impedance data. The experimental data are from 6.0 to 6.1 GHz in the 200 configurations, and the theoretical data are numerically generated with the estimated loss parameter \( \alpha = 4.51 \). We use the Monte Carlo method to generate \( 2 \times 10^6 \) impedance matrix samples. The distributions for the real parts of \( z_{11} \) (experimental and theoretical) are centered at one, and the distributions for the imaginary parts of \( z_{11} \) (experimental and theoretical) are centered at zero. This is what would be expected since \( z \) is the normalized impedance, and on average, the port reactance should be zero, which is consistent with the RCM. The experimental and theoretical PDFs show very good agreement. Note that only one parameter (\( \alpha \)) is used to fit the PDFs. This demonstrates the applicability of the

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**Table I**

<table>
<thead>
<tr>
<th>Frequency Range (GHz)</th>
<th>( \alpha )</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.0–3.1</td>
<td>1.24</td>
</tr>
<tr>
<td>4.0–4.1</td>
<td>1.38</td>
</tr>
<tr>
<td>5.0–5.1</td>
<td>2.33</td>
</tr>
<tr>
<td>6.0–6.1</td>
<td>4.51</td>
</tr>
<tr>
<td>7.0–7.1</td>
<td>6.19</td>
</tr>
<tr>
<td>8.0–8.1</td>
<td>7.99</td>
</tr>
<tr>
<td>9.0–9.1</td>
<td>9.31</td>
</tr>
<tr>
<td>10.0–10.1</td>
<td>10.93</td>
</tr>
</tbody>
</table>

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RMT in describing the universal properties of a complex 3-D enclosure, which has an electrically large port.

B. Radiation Scattering of the GigaBox, $S_{\text{rad}}$

The radiation scattering matrix, which is denoted as $S_{\text{rad}}$, of the GigaBox was obtained by a free space measurement of the scattering matrix. The source frequency for the measurement was from 3 to 10 GHz. The free space radiation setup for the GigaBox was done by placing the GigaBox in an anechoic chamber, and removing all of its walls except for the two walls that are used to mount the two antennas (see Fig. 3). The setup is such that there is free space radiation between the two ports while closely maintaining near-field characteristics of the ports. The side walls used in our $S_{\text{rad}}$ measurement, Fig. 3, were finite in size, however, numerical simulation showed that the frequency characteristics were unperturbed. Comparing with the setup in Fig. 1, the short-trajectory coupling, which represents the short trajectories bouncing in the enclosure, is removed from the free space measurement of $S_{\text{rad}}$.

The ensemble-average matrix $\langle S_{\text{cav}} \rangle$ was calculated by averaging 200 cavity scattering matrices, which are measured in the cavity shown in Fig. 1. Fig. 4 shows the comparison between the magnitudes of $S$ matrix elements (i.e., $|S_{11}|$, $|S_{22}|$, and $|S_{12}|$) of $S_{\text{rad}}$ and $\langle S_{\text{cav}} \rangle$ over the frequency range from 3 to 10 GHz. As predicted by the RCM, the radiation scattering elements, which represent the system-specific feature of the ports, follow the trend of the ensemble-averaged elements [10], [16]. The deviation between $S_{\text{rad}}$ and $\langle S_{\text{cav}} \rangle$ can be understood as the short-trajectory coupling effect introduced by Hart et al. [17], [18]. $\langle S_{\text{cav}} \rangle$ combines the radiation scattering matrix, $S_{\text{rad}}$, and the effects of short trajectories remaining after the ensemble average. Previous work on the RCM [17], [18] has examined the effects of utilizing either $S_{\text{rad}}$ or $\langle S_{\text{cav}} \rangle$ to convert to an impedance matrix and do the impedance normalization [see (3)]. Generally, utilizing $\langle S_{\text{cav}} \rangle$ makes the RCM more complete in describing the system and brings about better results in statistical predictions. The improvement is significant when the measured frequency range is small and cannot cover the corresponded frequency range of the shortest trajectory. Therefore, in this paper, we only use $\langle S_{\text{cav}} \rangle$ for the RCM analysis.

C. Comparison of RCM PDFs and Experimental PDFs of the Induced Voltages on the Conductor in the GigaBox

We have shown that the RCM can well describe the universal fluctuating feature and the system-specific feature of the impedance matrix (or the scattering matrix) of a complex enclosure. Now we consider the application to the induced voltage on the long port. We imagine that a pulse of electromagnetic energy enters the enclosure through port 1, and we wish to estimate the distribution of voltages present on port 2. The PDF of induced voltages on port 2 is valuable information for assessing the risks of electromagnetic interference on the electrically long
port, which represents a long cable in an enclosure. The PDF of induced voltages on a port can be directly obtained from experimental measurement of the impedance matrices from the 200 configurations of the GigaBox [9]. However, it is interesting to see if this PDF can be predicted numerically using the RCM for several frequency windows.

For a given frequency window, the loss parameter $\alpha$, and the ensemble-averaged impedance matrix $\langle Z_{\text{cav}} \rangle$ of the GigaBox, were determined experimentally; see Fig. 5.

The loss parameter was then used to generate an ensemble of random normalized impedances, $z_{\text{RMT}}$, using the RMT. The ensemble of $z_{\text{RMT}}$, which were generated by the Monte Carlo method [see (6)], and the $\langle Z_{\text{cav}} \rangle$ of the GigaBox, which is solely a property of the ports, were used to predict the ensemble of theoretical impedance by using (2) and replacing $z$ with $z_{\text{RMT}}$; see Fig. 6.

From this ensemble of numerically generated impedance, the numerical PDF of the induced voltages was generated [9].

In the experiments, both ports were connected to the network analyzer for measurement of the scattering matrix. In that case, the ports are terminated with the characteristic impedance (50 $\Omega$), and therefore, no reflection comes back from the transmission lines. In practice, there may be a load impedance, $Z_L$, on port 2, and the voltages induced on that port may be generated by directly using the measured cavity impedance without any numerically generated normalized impedance, $z$, utilizing [11]

$$|V| = \sqrt{ \frac{2P_1(f)|Z_p|^2|Z_{\text{cav}}^\text{av}|^2}{\text{Re}[Z_{11}^\text{cav}]} }$$  \hspace{1cm} (7)

where

$$Z_p = \frac{Z_{21}^\text{cav} Z_L/Z_{eq}}{Z_{22}^\text{cav} + Z_L} \quad \text{and} \quad Z_{eq} = Z_{cav}^\text{av} - \frac{Z_{21}^\text{cav} Z_{22}^\text{cav} + Z_L}{Z_{22}^\text{cav} + Z_L}. \hspace{1cm} (8)$$

The radiated power spectrum of port 1, $P_1(f)$, is assumed to be constant in frequency windows of 100-MHz bandwidth. We may also assume a special case that the load impedance $Z_L$ on port 2 approaches infinity (open circuit on port 2). In this case, the experimental PDFs of the induced voltages $|V|$ may be calculated as

$$|V| = \sqrt{ \frac{2P_1(f)|Z_{21}^\text{cav}|^2}{\text{Re}[Z_{11}^\text{cav}]} }.$$  \hspace{1cm} (9)

Here, we demonstrate results from four different frequency windows, which have their own distinct loss parameter value. These are 3.0–3.1 GHz (with $\alpha = 1.24$), 5.0–5.1 GHz (with $\alpha = 2.33$), 7.0–7.1 GHz (with $\alpha = 6.19$), and 10.0–10.1 GHz (with $\alpha = 10.93$).

D. Independence of Voltage Distributions on Port Locations

The distribution of the induced voltages on the target (port 2) should be independent of the location of the energy transmitting source (port 1), when the off-diagonal components of $\langle Z_{\text{cav}} \rangle$ are negligible compared to the diagonal components of $\langle Z_{\text{cav}} \rangle$ according to (4) [11]. For example, this is true when the ports are far apart or the major short trajectories are blocked. Also, the distribution should be independent of source locations because the E-fields in the cavity (as a reverberation chamber), due to the ray-chaotic nature, should have random polarizations and incidences resulting in similar distributions.

An experiment was carried out to investigate this hypothesis. The monopole antenna at port 1 was moved from its original location to the alternative location, which is also shown in Fig. 1 (which is 0.3 m away from the original location of port 1 horizontally, and 0.076 m away vertically). We plot the PDFs of induced voltages computed experimentally by (9) setting $Z_L \to \infty$. Fig. 8 shows little difference in the results of the measured PDFs of induced voltage from 8.0 to 8.1 GHz. This demonstrates that the statistics of induced voltage are dictated by a single property of the enclosure—the loss parameter, in addition to the radiation impedance matrix of the ports (or the ensemble-averaged impedance matrix of the ports [17], [18]).
Therefore, once the loss parameter is determined, it can be applied when the enclosure configuration is changed. This condition is constrained to the case of uniform loss in the enclosure. Future RCM work will focus on external radiation into a large cavity with an aperture. The introduction of large apertures, which become the dominant source of loss in the enclosure, would cause the voltage distributions due to different transmitting locations to deviate.

V. CONCLUSION

The experimental results demonstrate that the RCM can be applied to a large, 3-D enclosure, which has an electrically large port, for statistical predictions of electromagnetic fields. The applicability of the RMT to the 3-D cavity is also verified. The existence of universal fluctuations in the 3-D cavity was shown through experimental results. The ability to obtain \( \langle Z_{\text{cav}} \rangle \) by averaging the measured cavity impedance matrices \( Z_{\text{cav}} \) avoids the impractical free space measurement of large and complicated cavities. We examined the radiation scattering matrix \( S_{\text{rad}} \) of the 3-D enclosure, which should follow the trend of the ensemble-averaged scattering matrix \( \langle S_{\text{cav}} \rangle \) as in previous RCM research [17], [18]. In this paper, we focused on \( \langle S_{\text{cav}} \rangle \), which better describes the system-specific features of the wave enclosure. We summarized the RCM process of utilizing the experimental data to obtain the loss parameter \( \alpha \) (in Fig. 5) and the RCM process of generating numerical predictions of \( Z_{\text{cav}} \) by \( \alpha \) and \( \langle Z_{\text{cav}} \rangle \) (in Fig. 6). PDFs of the induced voltages on the electrically large port in the cavity, which are numerically calculated by the RCM, closely match their experimental PDF counterparts.

For generating the numerical predictions by the RCM, one needs to determine the loss parameter of the system, and the system-specific features as \( \langle Z_{\text{cav}} \rangle \). In this paper, we used the 200 measured \( Z_{\text{cav}} \) realizations to determine the loss parameter (in Section III-B) and to calculate \( \langle Z_{\text{cav}} \rangle \) (in Section IV-B). It is worth noting that there are alternative ways to determine these two factors. For example, the loss parameter can be calculated directly from first principles with the quality factor as (4). For the ensemble-averaged impedance matrix \( \langle Z_{\text{cav}} \rangle \), Hart et al. [17], [18] have introduced the short-trajectory correction to synthesize the approximation of \( \langle Z_{\text{cav}} \rangle \) by utilizing the geometry of the enclosure.

The prediction of induced voltage on the conductor is also shown to be independent of the transmitting port location.

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